

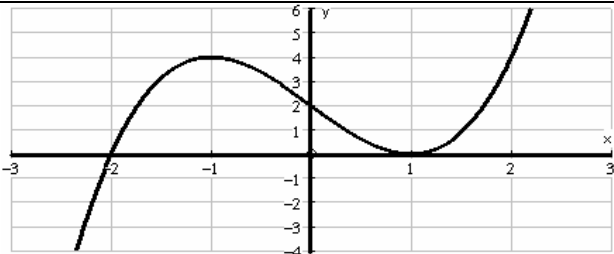
MEI STRUCTURED MATHEMATICS

CONCEPTS OF ADVANCED MATHEMATICS, C2

Practice Paper C2-A

MARK SCHEME

Qu	Answer	Mark	Comment
Section A			
1	$\frac{dy}{dx} = 2 - 5x$ $\Rightarrow y = 2x - \frac{5}{2}x^2 + c$ <p>When $x = 0, y = 1$</p> $\Rightarrow 1 = c \Rightarrow y = 2x - \frac{5}{2}x^2 + 1$	M1 A1 M1 A1	4
2	(i) $\log_2 5 + \log_2 1.6 = \log_2 5 \times 1.6$ $= \log_2 8 = 3$	M1 A1	2
	(ii) $2^x = 3 \Rightarrow x \ln 2 = \ln 3$ $\Rightarrow x = \frac{\ln 3}{\ln 2}$ ≈ 1.5850	M1 A1 A1	3
3	(i) A.P.: $5 + 8 + 11 \dots$ $\Rightarrow a_8 = 5 + 7 \times 3 = \pounds 26$	M1 A1	2
	(ii) We require $S_n > 200$ so solve $S_n = 200$ $S_n = \frac{n}{2}(2a + (n-1)d) = \frac{n}{2}(10 + (n-1)3) = 200$ $\Rightarrow 10n + 3n(n-1) = 400 \Rightarrow 3n^2 + 7n - 400 = 0$ $\Rightarrow n = \frac{-7 \pm \sqrt{49 + 4800}}{6} = \frac{-7 \pm 69.6}{6} = 10.4$ So minimum time is 11 years.	M1 A1 M1 A1	4
4	$\frac{dy}{dx} = 3x^2 + 2$ <p>When $x = 0, \frac{dy}{dx} = 2 \Rightarrow y - 7 = 2(x - 0)$</p> $\Rightarrow y = 2x + 7$	B1 B1 M1 A1	4
5	(i) $2 \sin^2 \theta + 3 \cos \theta = 2 - 2 \cos^2 \theta + 3 \cos \theta$	B1	1
	$2 \sin^2 \theta + 3 \cos \theta = 3 \Rightarrow 2 - 2 \cos^2 \theta + 3 \cos \theta = 3$ $\Rightarrow 2 \cos^2 \theta - 3 \cos \theta + 1 = 0$ $\Rightarrow (2 \cos \theta - 1)(\cos \theta - 1) = 0 \Rightarrow \cos \theta = 1, \frac{1}{2}$ $\Rightarrow \theta = 0^\circ, 60^\circ, 300^\circ, 360^\circ$	B1 M1 A1 A1	For 0,60,360 For 300 5

6	(i)	$s = r\theta \Rightarrow r = \frac{45}{2} = 22.5 \text{ (cm)}$	M1 A1 2	
	(ii)	$A = \frac{1}{2}r^2\theta = 22.5^2 = 506.25 \text{ (cm}^2\text{)}$	M1 A1 2	
7	(i)	$S_{10} = a \frac{1-r^{10}}{1-r}; r = 0.8, a = 5$ $\Rightarrow S_{10} = 5 \frac{1-0.8^{10}}{0.2} = 22.32$	M1 A1 2	
	(ii)	$S_{\infty} = a \frac{1}{1-r} = 25$	B1 1	
8		$BC^2 = 5^2 + 6^2 - 2 \times 5 \times 6 \times \cos 110$ $= 61 + 20.52 = 81.52$ $\Rightarrow BC = 9.03 \text{ cm}$	M1 A1 B1 A1 A1 5	For getting neg for cos110
Section B				
9	(i)	Multiply out to get $x^3 - 3x + 2$	M1 A1 2	
	(ii)	$y = x^3 - 3x + 2 \Rightarrow \frac{dy}{dx} = 3x^2 - 3$ $\frac{dy}{dx} = 0$ when $x = \pm 1$ $\frac{d^2y}{dx^2} = 6x;$ when $x = -1, \frac{d^2y}{dx^2} < 0$ so maximum when $x = 1 \frac{d^2y}{dx^2} > 0$ so minimum. when $x = 1, y = 0$	M1 A1 M1 M1 E1 M1 B1 7	
	(iii)		B1 1	
	(iv)	For values of k within max and min values of y there are three roots. When $x = -1, y = 4$ i.e. $k < 0$ and $k > 4$	M1 B1 A1 3	

